

Review of recent theoretical developments in Higgs physics

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**Xth Quark Confinement and the Hadron Spectrum
Munich, October 2012**



After the euphoria

- Three months ago, the announcement of the Higgs discovery generated great excitement



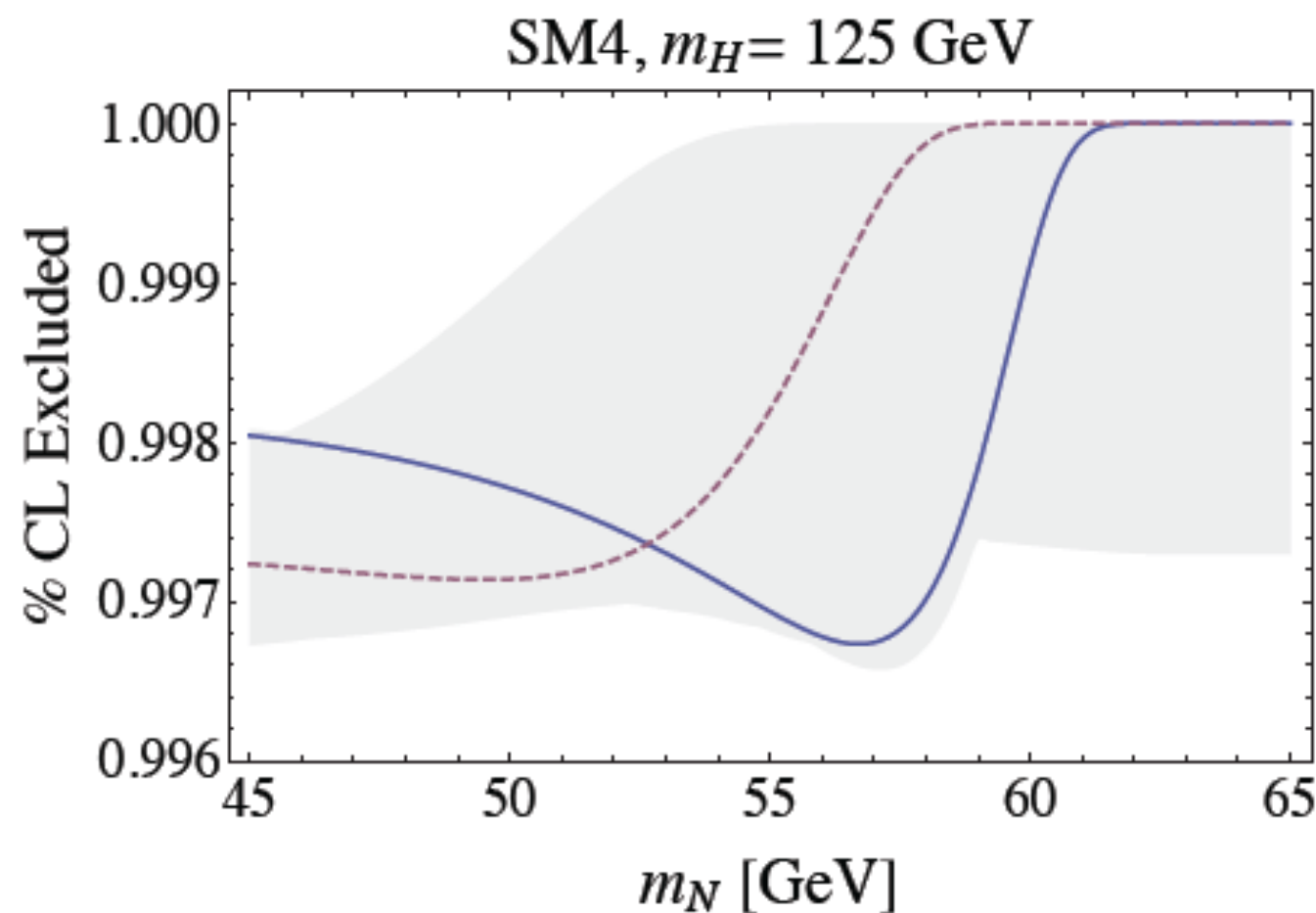
- With the excitement over (or at least reduced), it's now time to analyze the discovery
- Is it the Standard Model Higgs, or do its couplings deviate?
- In fact, is it even a Higgs boson, or could it be something else (a spin-2 state, or a CP-odd scalar, or ...)?
- Is theory in shape to distinguish between these possibilities?

Discovery is the beginning

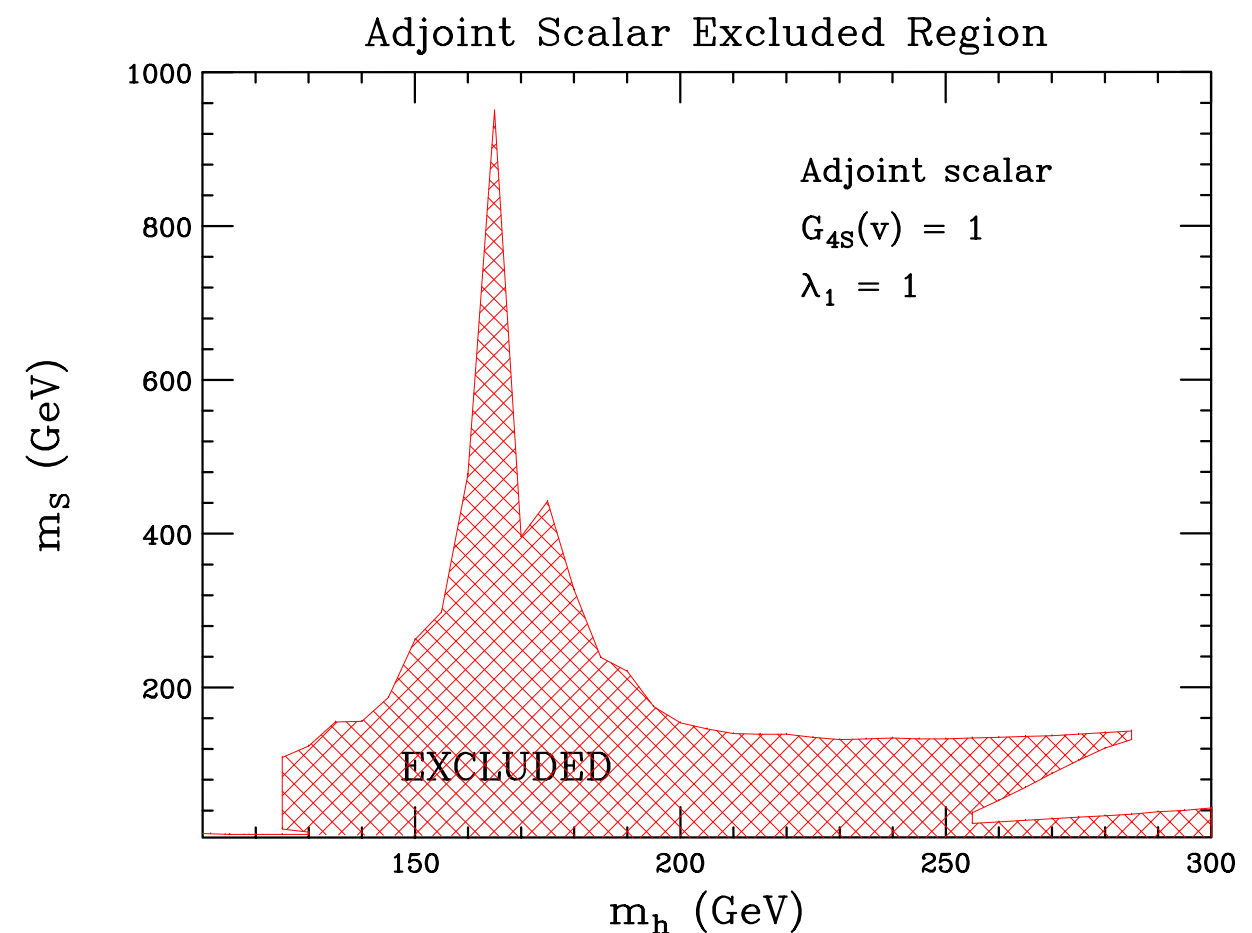


Narrowing down the possibilities

- Current measurements already strongly constrain what SM extensions are possible



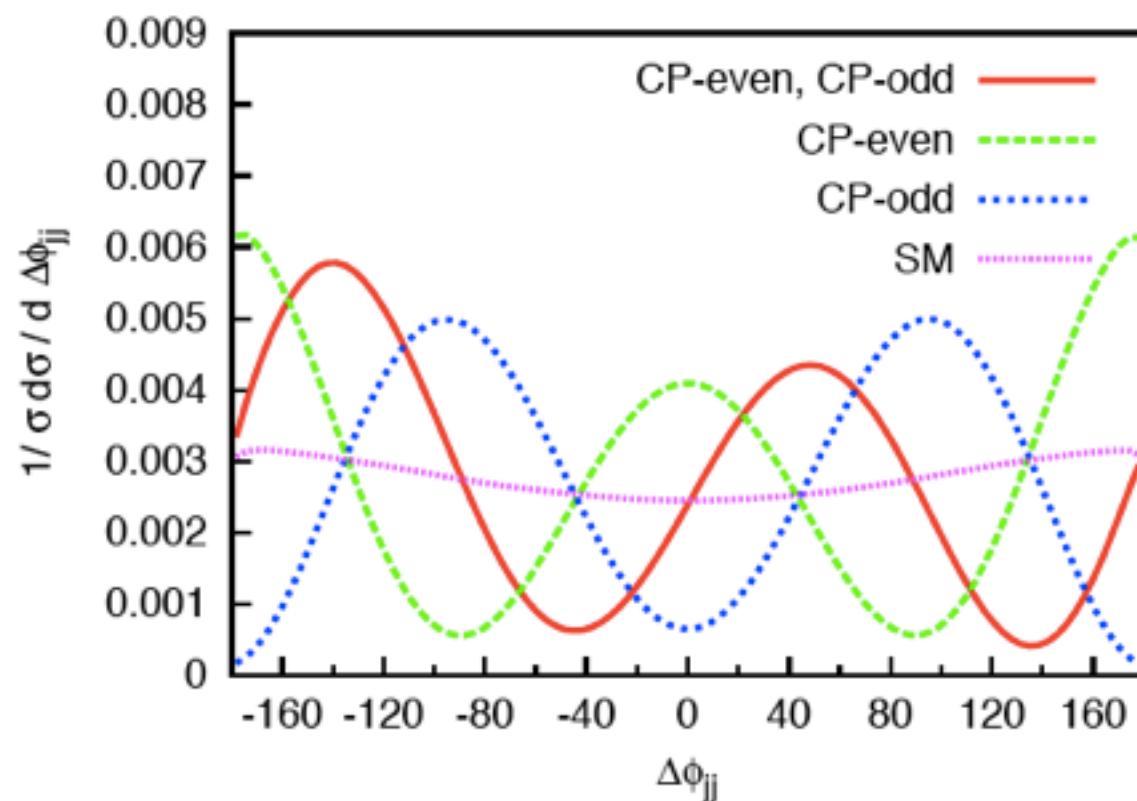
Kuflik, Nir, Volansky 2012



R. B. 2011

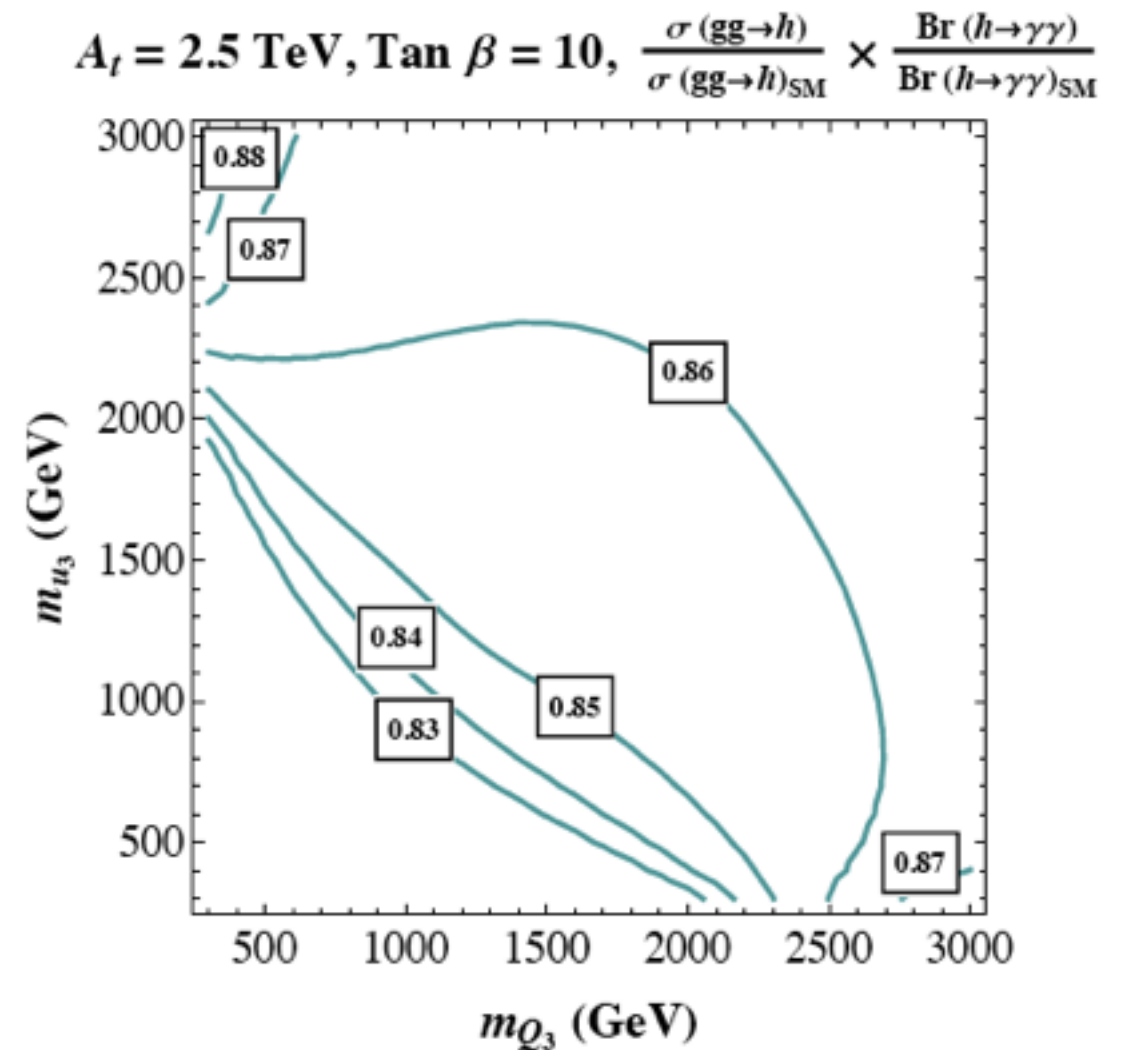
Measuring Higgs properties

- To pin down the underlying model, what are we interested in measuring?



Angular distributions, of either jets or decay products

Zeppenfeld et al. 2006



The rate

Carena, Gori, Shah, Wagner 2011

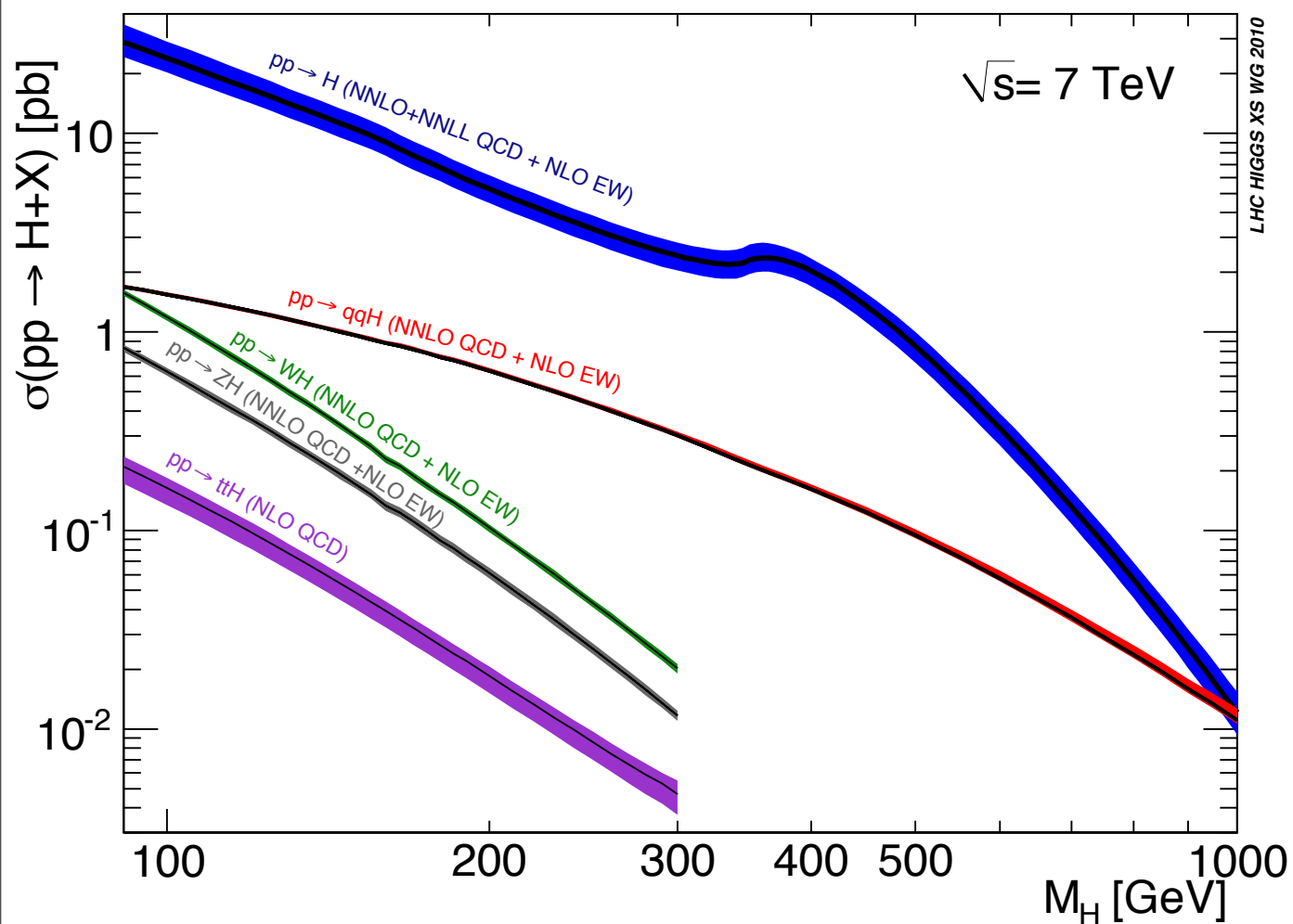
Effects of theory uncertainties

- CMS PAS HIG-11-024: (WW channel) “The overall signal efficiency uncertainty... is dominated by the theoretical uncertainty due to missing higher-order corrections”
- ATLAS CERN-PH-EP-2012-013 ($\gamma\gamma$): uncertainties due to QCD scale variation one of the two dominant systematic effects (along with photon reconstruction+ID efficiency)

Source	Affected Processes	Typical uncertainty
PDFs+ α_s (cross sections)	$gg \rightarrow H, t\bar{t}H, gg \rightarrow VV$ VBF H, VH, VV @NLO	$\pm 8\%$ $\pm 4\%$
Higher-order uncertainties on cross sections	total inclusive $gg \rightarrow H$ inclusive “ gg ” $\rightarrow H + \geq 1$ jets inclusive “ gg ” $\rightarrow H + \geq 2$ jets VBF H associated VH $t\bar{t}H$ uncertainties specific to high mass Higgs boson, see Section 2.1 V VV up to NLO $gg \rightarrow VV$ $t\bar{t}$, incl. single top productions for simplicity	$+12\%$ -7% $\pm 20\%$ $\pm 20\%$ (NLO), $\pm 70\%$ (LO) $\pm 1\%$ $\pm 1\%$ $+4\%$ -10% $\pm 30\%$ $\pm 1\%$ $\pm 5\%$ $\pm 30\%$ $\pm 6\%$
acceptance	acceptance for $H \rightarrow WW \rightarrow \ell\nu\ell\nu$ events	$\pm 2\%$
phenomenology	modelling of underlying event and parton showering fake lepton probability ($W + jets \rightarrow \ell\ell^{fake}$)	$\pm 10\%$ $\pm 40\%$
luminosities	ATLAS and CMS uncertainties on their luminosity measurements	$\pm 3.7\%$, $\pm 4.5\%$

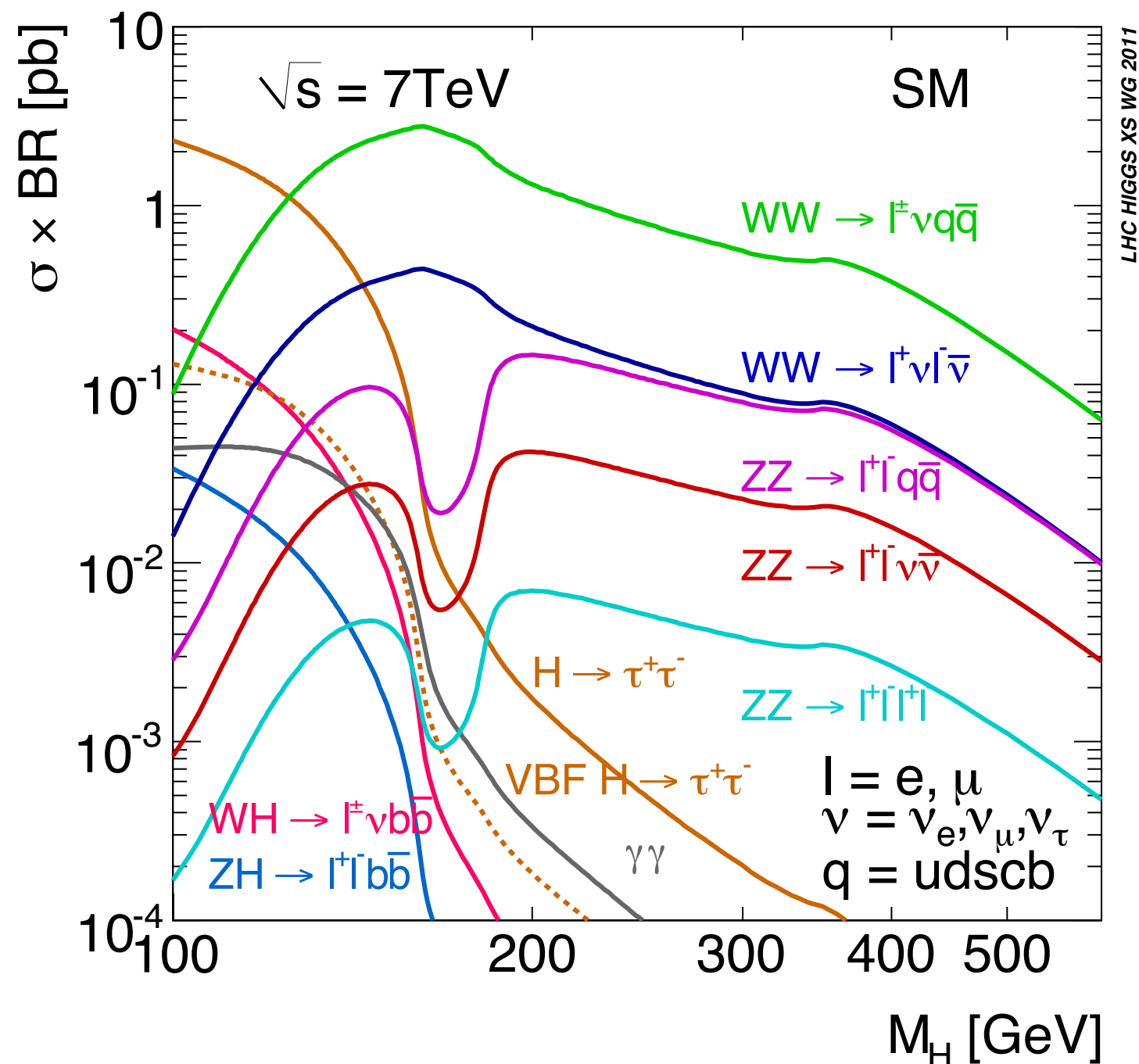
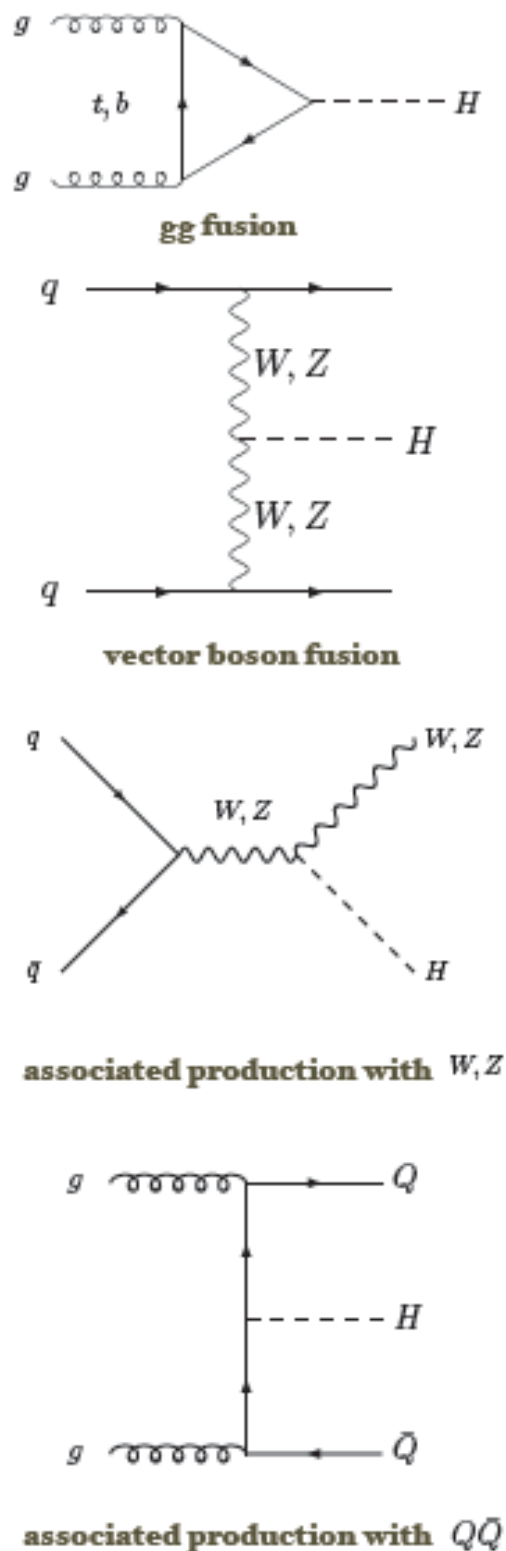
from G. Rolandi,
HCP 2011

Outline



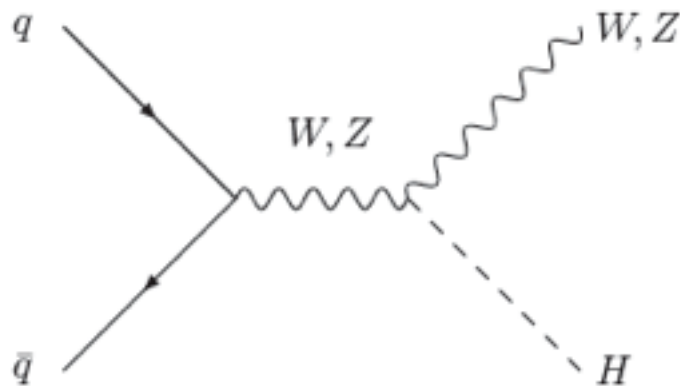
- Review the theory going into the Higgs analysis
- Discuss available tools, some of the tricky points in the calculations
- Brief summary of VH, VBF
- Longer discussion of gluon-fusion and its backgrounds; much recent work and still some unresolved issues in this analysis
- Measurement of Higgs properties

A phenomenological profile



For SM Higgs, production primarily from $gg \rightarrow H$, with some contribution from VBF (VH for b Yukawa measurement)

Associated VH production

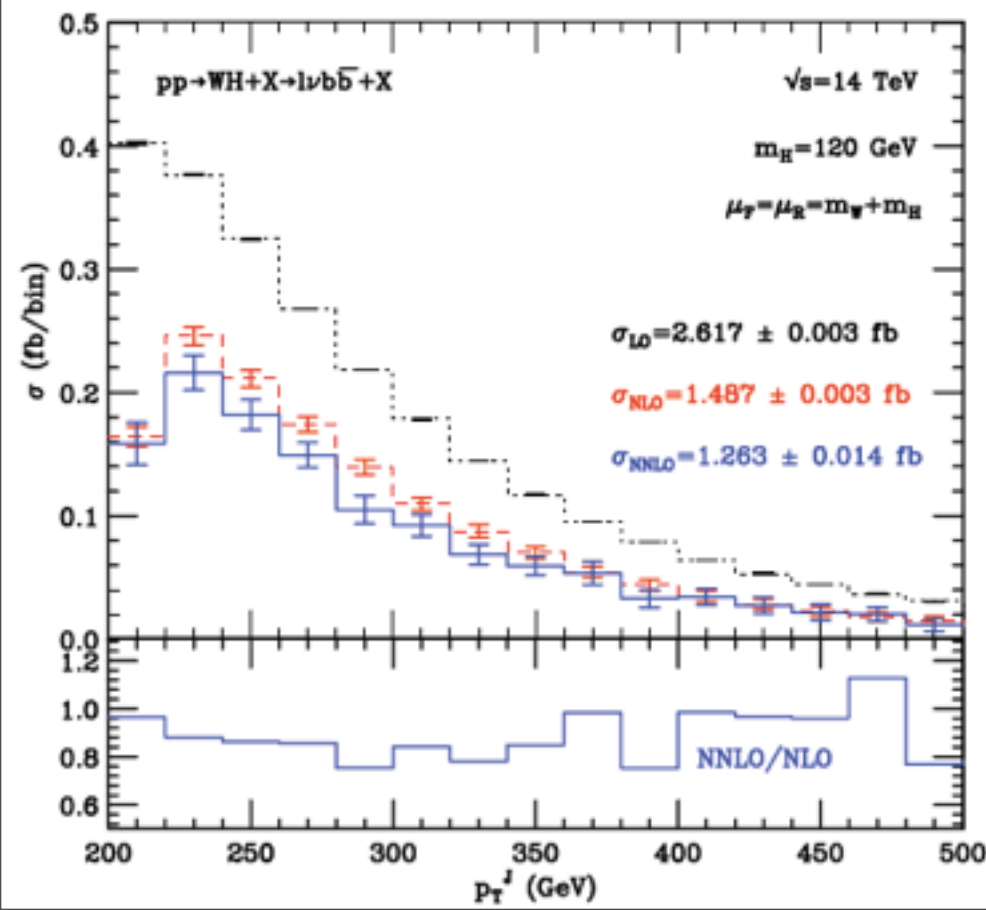


- With $b\bar{b}$ decay of Higgs, most important low-mass mode at Tevatron
- At LHC, boosted analysis possible

Butterworth, Davison, Rubin, Salam 2008

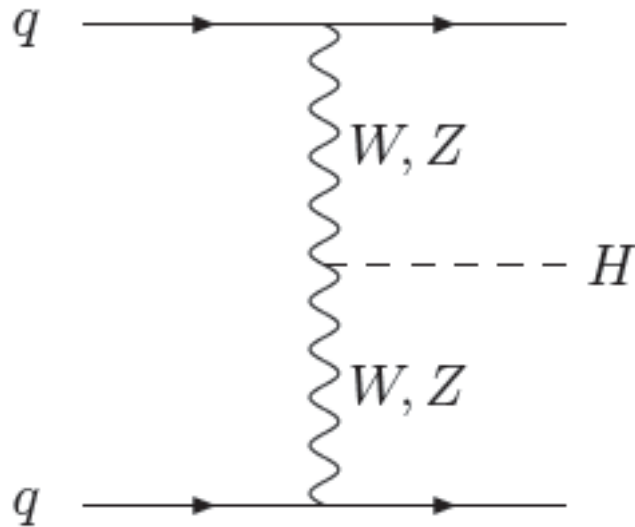
Inclusive NLO QCD: +30% (Han, Willenbrock 1990), NLO EW: +5-10% (Ciccolini, Dittmaier, Denner 2003)

NNLO QCD: 1-2% in bulk of phase space (Ferrera, Grazzini, Tramontano 2011)



- Original boosted analysis vetoes additional jets to remove $t\bar{t}$ background
- Negative impact on stability of expansion (jet vetoes are theoretically dangerous!)
- Original paper mentions possibility of top-veto instead, likely safer from QCD perspective

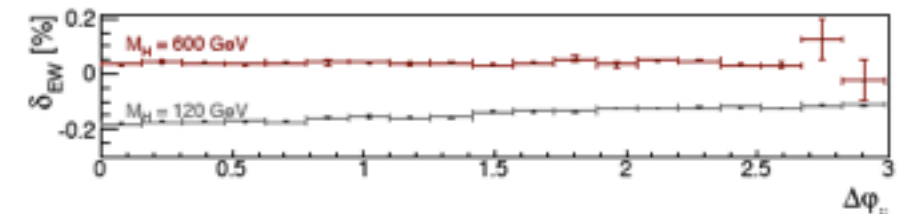
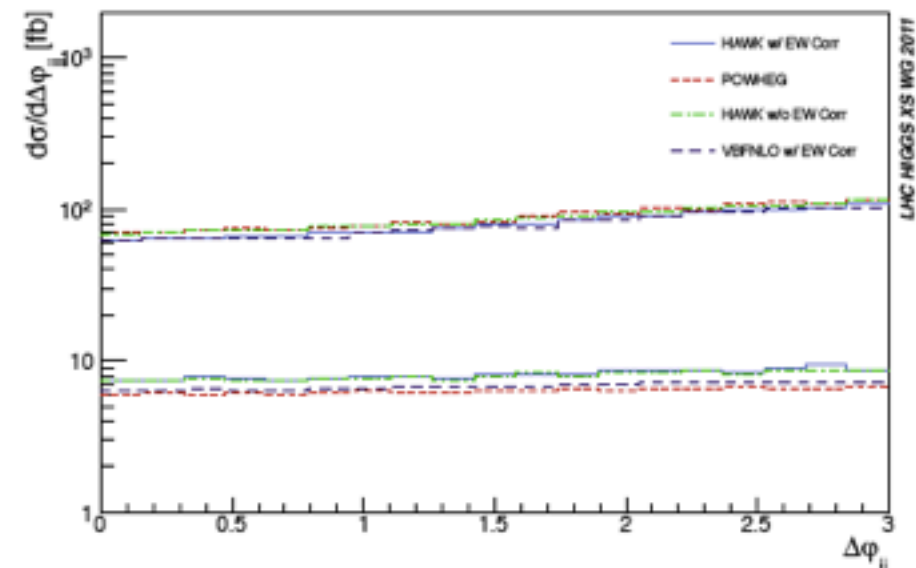
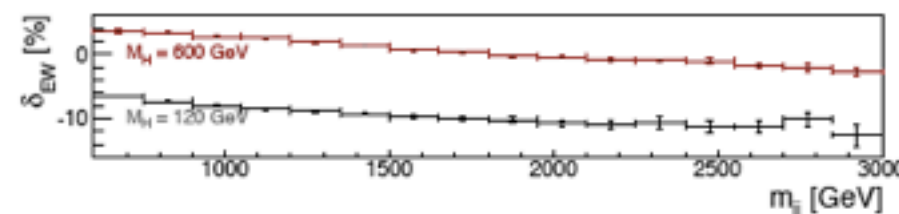
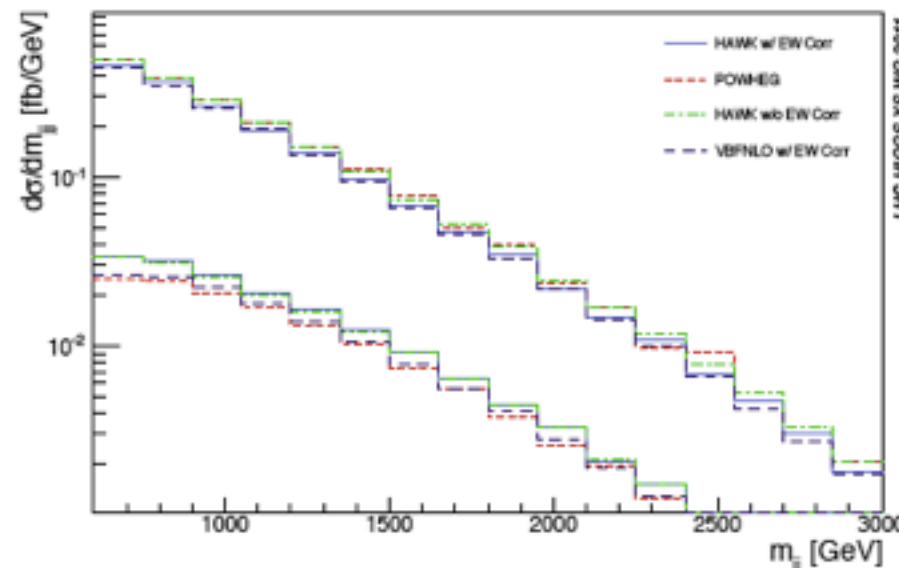
Vector boson fusion



- Important for the low-mass Higgs in both the $\tau\tau$ and $\gamma\gamma$ modes
- NLO QCD the same as for DIS, increase by 5-10%
- NLO QCD+EW in VBFNLO (Oleari, Zeppenfeld et al., partial EW) and HAWK (Denner, Dittmaier, Mueck, full EW)

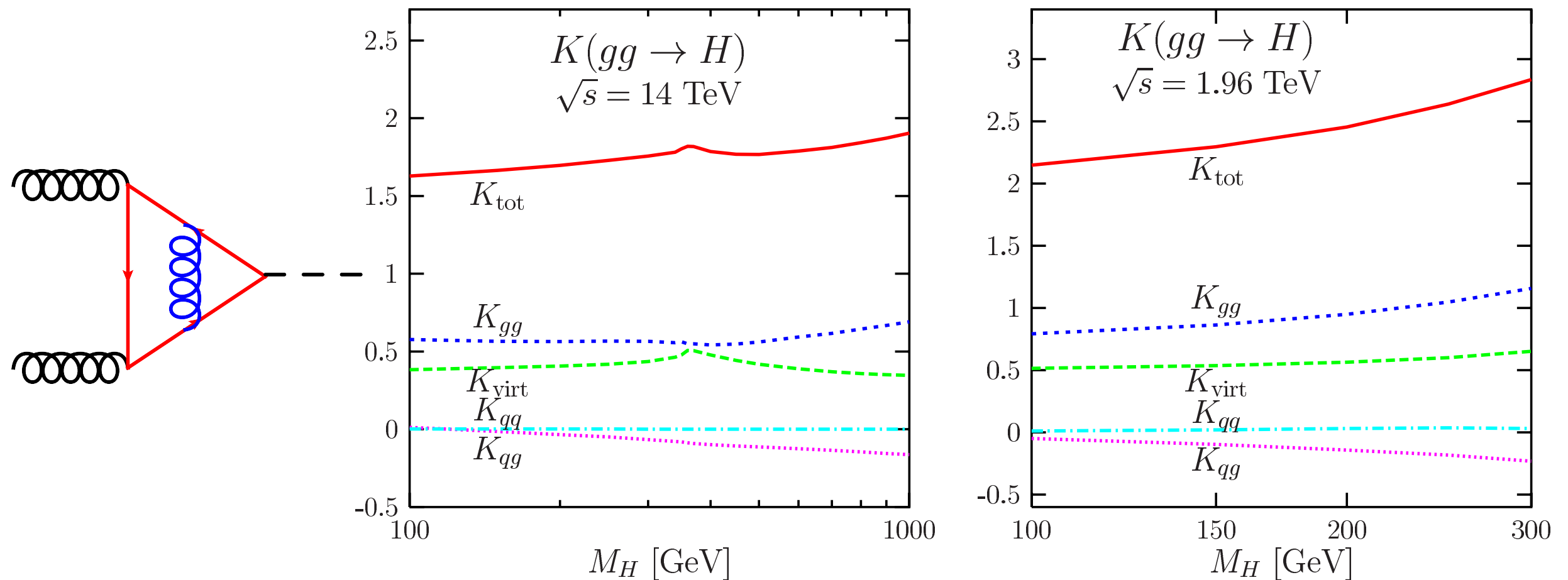
- DIS-like NNLO contributions also calculated, at the percent-level (Bolzoni, Maltoni, Moch, Zaro 2010)

- Important distributions under theoretical control



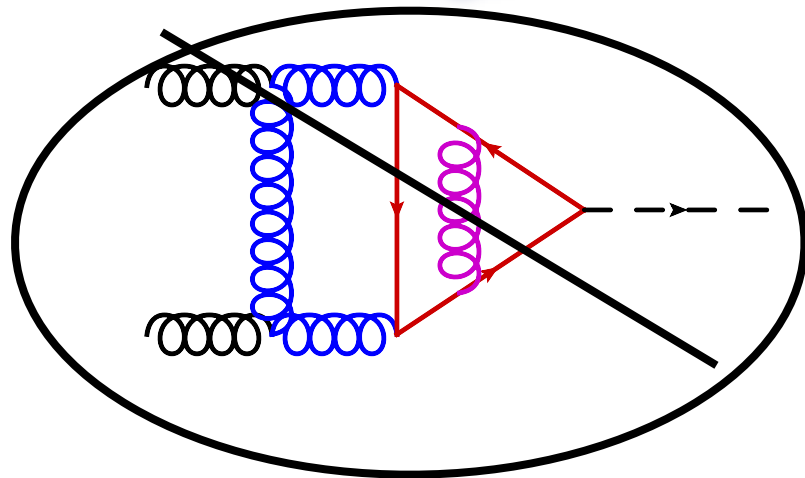
Gluon fusion

- Famously sensitive to large QCD corrections; difficult to calculate to requisite order in perturbation theory. The subject of enormous theoretical effort over the years.



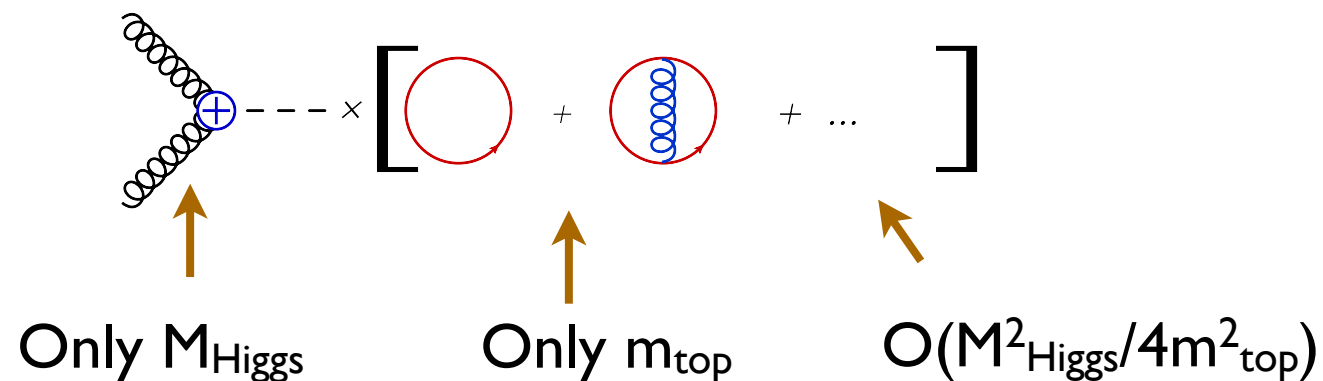
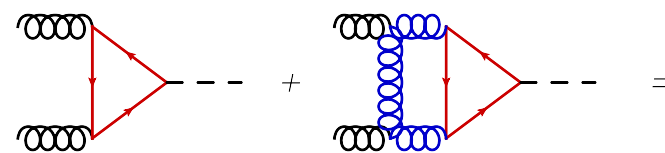
Dawson; Djouadi, Graudenz, Spira, Zerwas, 1991, 1995

Effective interactions



- Getting the next terms requires new techniques
- *Effective field theory*: exploit heavy mass of virtual particles

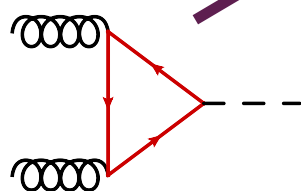
Two scales:
 $M_{\text{Higgs}}, m_{\text{top}}$



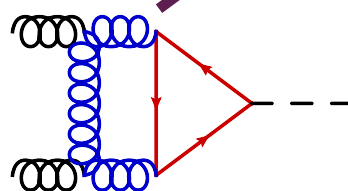
$$\mathcal{L}_{eff} = \alpha_s \frac{C_1}{4v} H G_{\mu\nu}^a G_a^{\mu\nu}$$

The Wilson coefficient

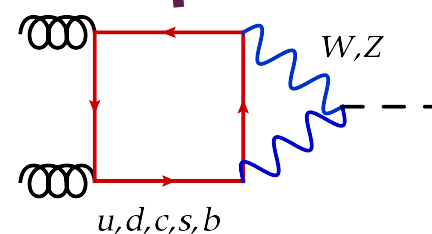
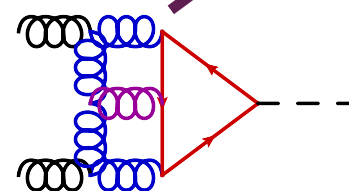
$$C_1 = -\frac{1}{3\pi} \left\{ 1 + \alpha_s C_{1t} + \alpha_s^2 C_{2t} + \lambda_{EW} [1 + C_{1w}] \right\}$$



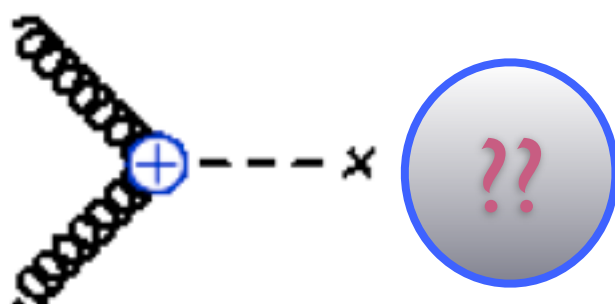
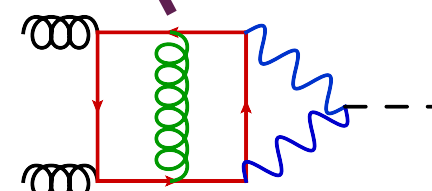
Inami, Kubota,
Okada 1982



Chetyrkin, Kniehl,
Steinhauser 1997



EW terms: Actis, Passarino, Sturm, Uccirati 2008;
Anastasiou, R. B., Petriello 2009



Clear separation of new physics
effects into Wilson coefficient, QCD
into corrections to the effective
vertex

Unreasonably effective EFT

NLO in the EFT:

analytic continuation to
time-like form factor

$$z = M_H^2 / (x_1 x_2 s)$$

$$\Delta\sigma = \sigma_0 \frac{\alpha_s}{\pi} \left\{ \left(\frac{11}{2} + \pi^2 \right) \delta(1-z) + 12 \left[\frac{\ln(1-z)}{1-z} \right]_+ - 12z(-z + z^2 + 2)\ln(1-z) - 6 \frac{(z^2 + 1 - z)^2}{1-z} \ln(z) - \frac{11}{2} (1-z)^3 \right\}$$

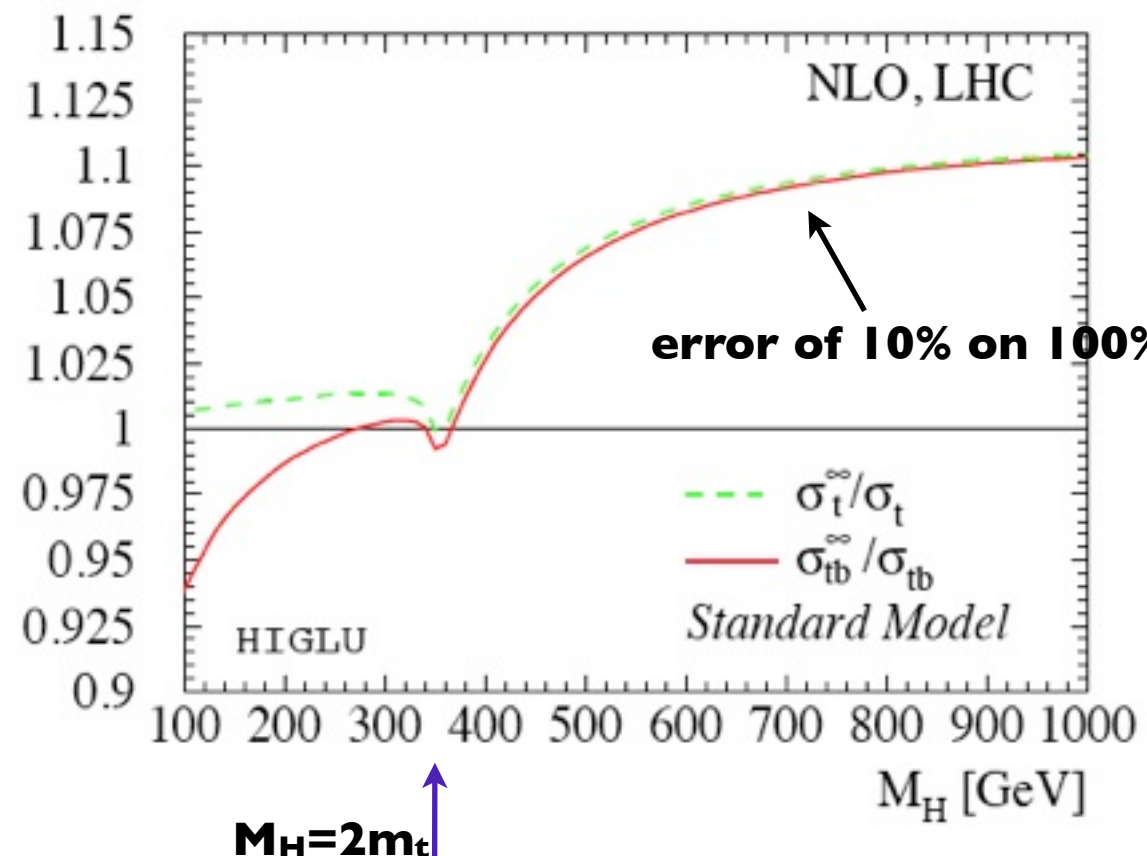
eikonal emission of soft gluons

Identical factors in full theory with $\sigma_0 \rightarrow \sigma_{LO, \text{full theory}}$

$$\sigma_{NLO}^{approx} = \left(\frac{\sigma_{NLO}^{EFT}}{\sigma_{LO}^{EFT}} \right) \sigma_{LO}^{QCD}$$

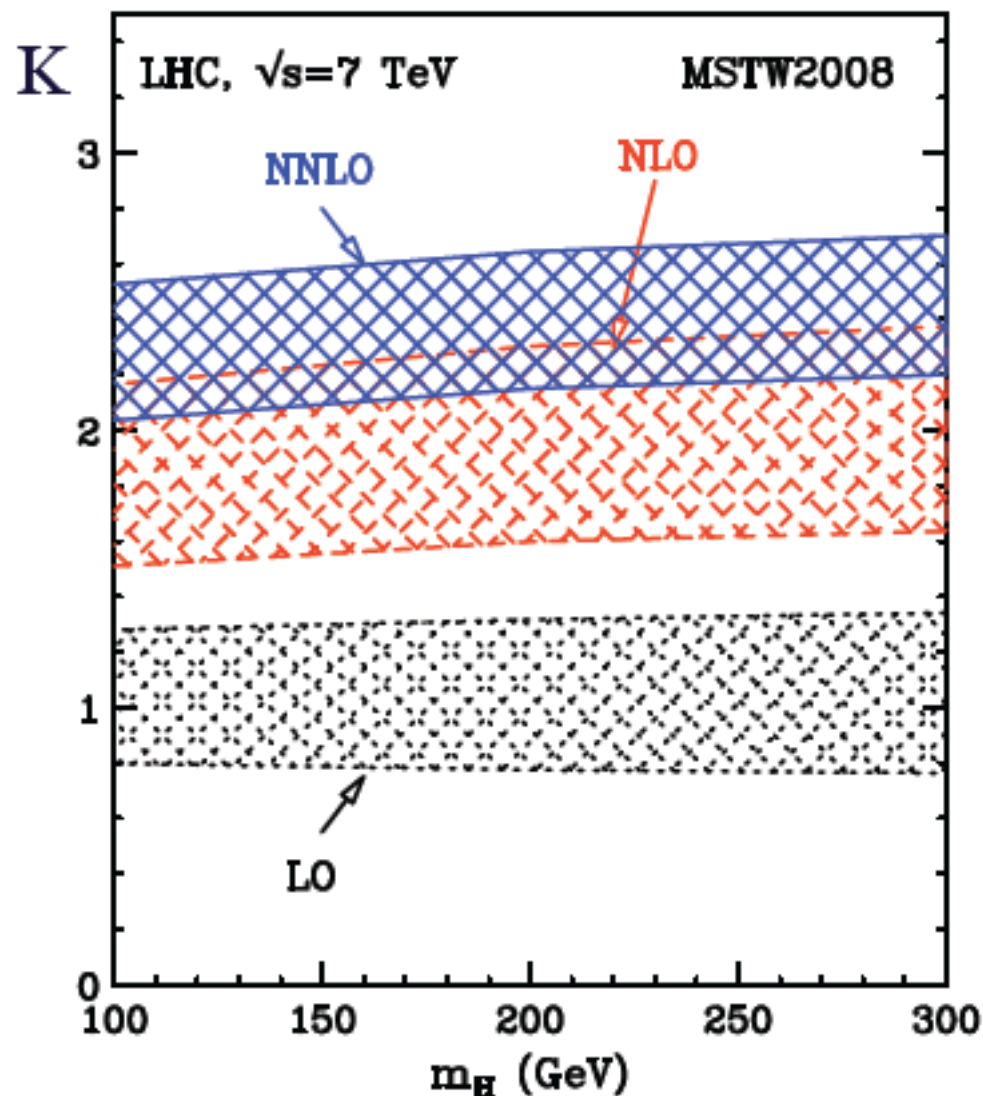
NNLO study of $1/m_t$ suppressed operators, matched to large \hat{s} limit, indicates this persists

Harlander, Mantler, Marzani, Ozeren; Pak, Rogal, Steinhauser 2009

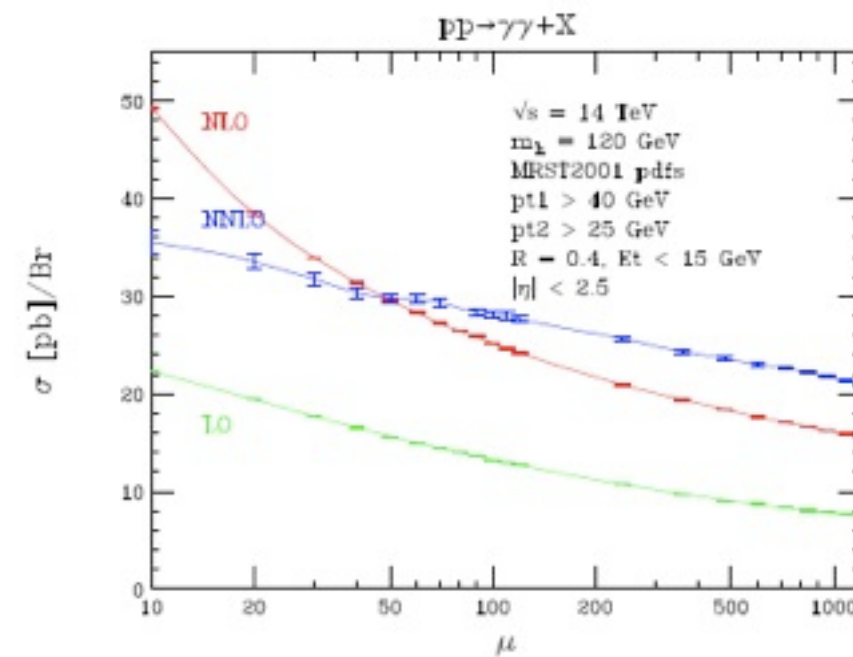


NNLO in the EFT

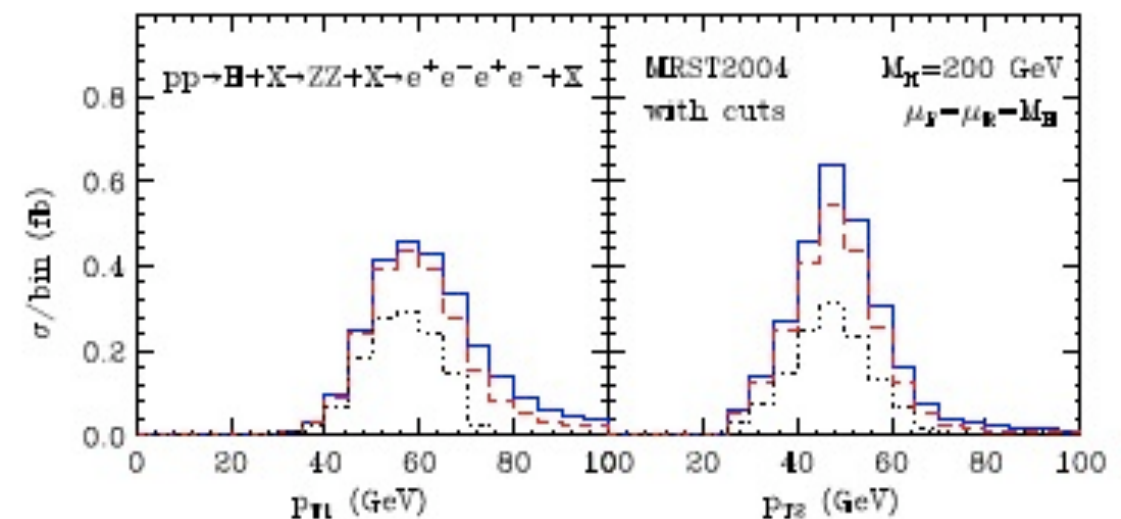
- Success of the EFT over almost entire interesting mass range motivates NNLO calculation



Harlander, Kilgore; Anastasiou, Melnikov;
Ravindran, Smith, van Neerven 2002-2003



FEHiP: Anastasiou, Melnikov, Petriello 2005



HNNLO: Catani, Grazzini 2007-2008

Gluon-fusion: inclusive

Effects of soft-gluon resummation at Next-to-next-to leading logarithmic (NNLL) accuracy (about 6-15%)

S. Catani, D. De Florian,
P. Nason, Grazzini (2003)

Partial N³LO corrections known (considerably reduced scale dependence)

Moch, Vogt (2005)

Two-loop EW corrections are also known (effect is about O(5%))

U. Aglietti et al. (2004)
G. Degrandi, F. Maltoni (2004)
G. Passarino et al. (2008)

Mixed QCD-EW effects evaluated in EFT approach

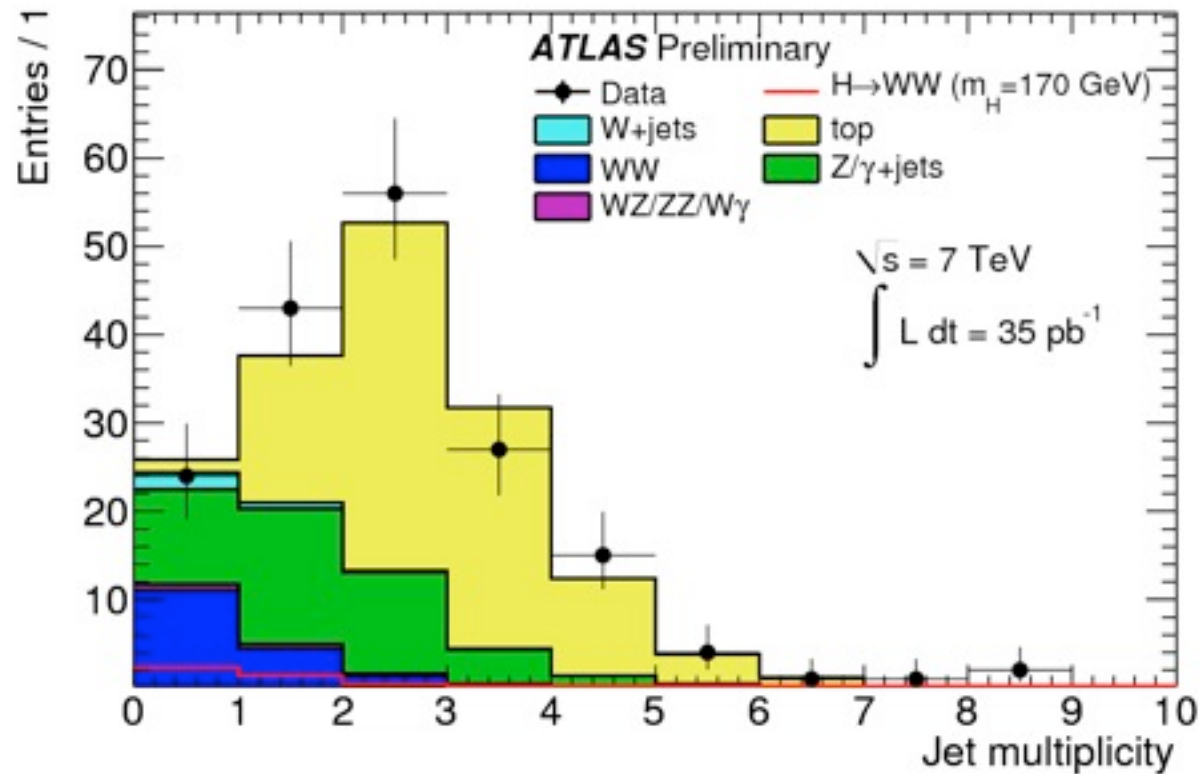
Anastasiou, R. B., Petriello (2008)

→ support “complete factorization”: EW correction multiplies the full QCD corrected cross section

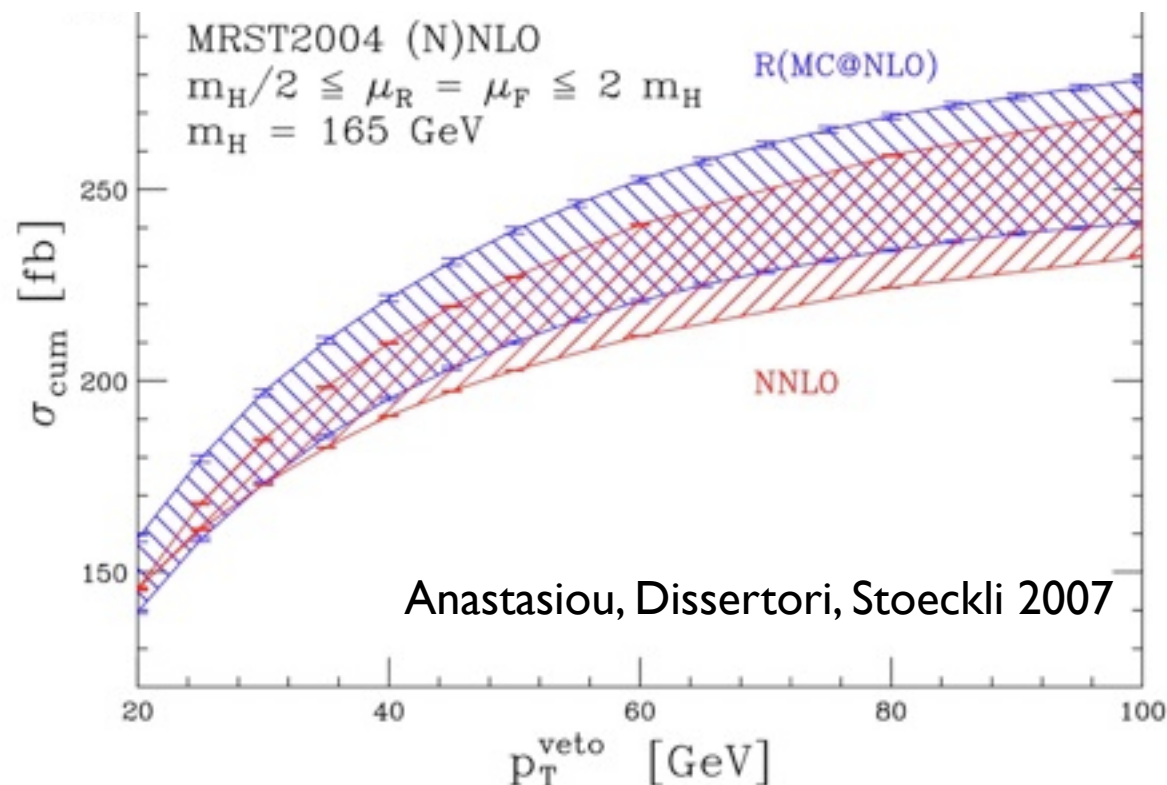
EW effects for real radiation (effect O(1%))

Keung, Petriello, (2009)
O. Brein, (2010)

The jet-veto in gluon fusion



- Toughest cut from theoretical perspective is the jet veto
- Required in WW channel due to background composition; also used in other channels to improve S/B
- 25-30 GeV jet cut used; restriction of radiation leads to large logs



- Inclusive scale variation 10%; with a 25 GeV jet veto, 5-6%!
- Having $\Delta\sigma_{\text{veto}} < \Delta\sigma_{\text{tot}}$ doesn't seem correct; σ_{veto} has a more complicated structure and a larger expansion parameter, $\alpha_s \ln^2(m_H/p_{T,\text{cut}})$ rather than α_s

Cancellations

- Study of cross section structure (Stewart, Tackmann 2011)

$$\begin{aligned}\sigma_0(p^{\text{cut}}) &= \sigma_{\text{total}} - \sigma_{\geq 1}(p^{\text{cut}}) \\ &\simeq \sigma_B \left\{ [1 + \alpha_s + \alpha_s^2 + \mathcal{O}(\alpha_s^3)] - [\alpha_s(L^2 + L + 1) + \alpha_s^2(L^4 + L^3 + L^2 + L + 1) + \mathcal{O}(\alpha_s^3 L^6)] \right\}\end{aligned}$$

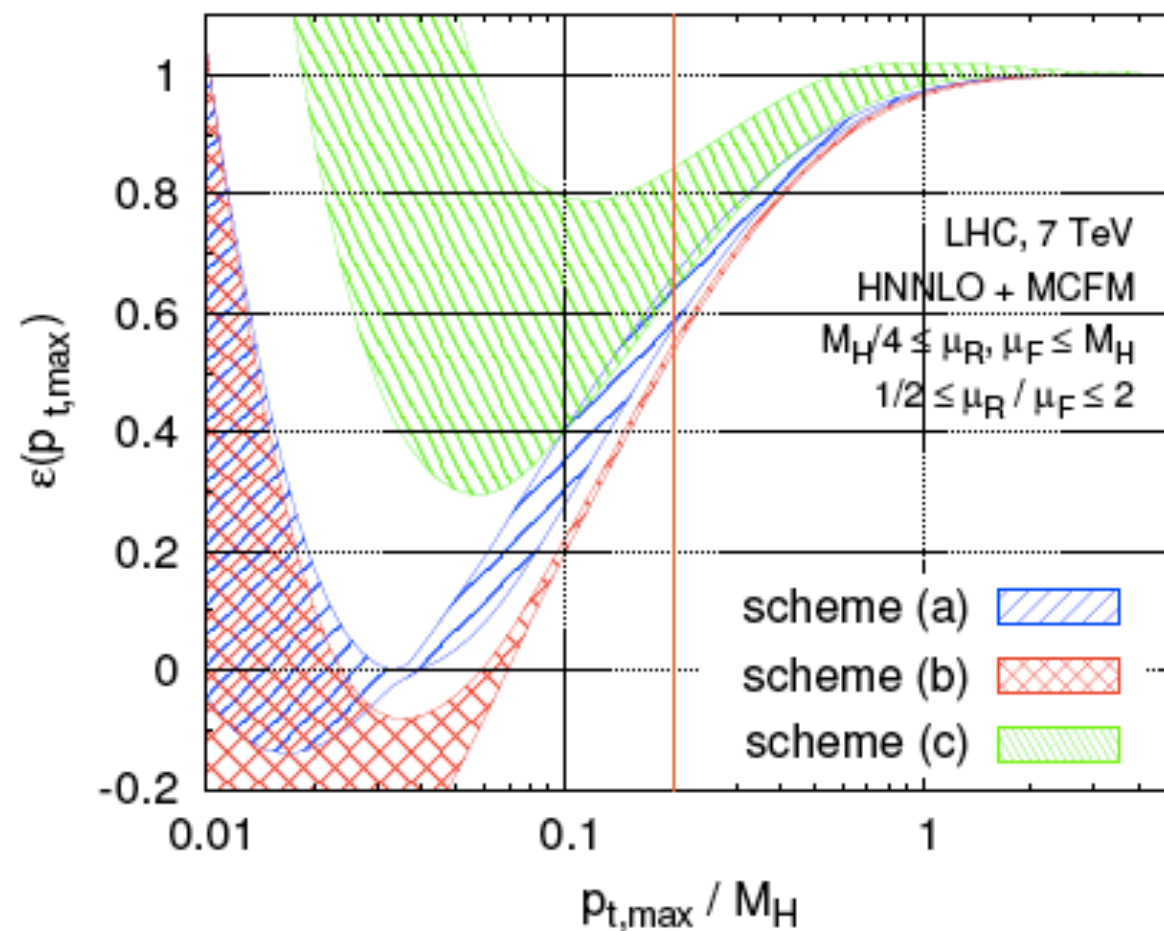
$$\sigma_{\text{total}} = (3.32 \text{ pb}) [1 + 9.5 \alpha_s + 35 \alpha_s^2 + \mathcal{O}(\alpha_s^3)] ,$$

$$\sigma_{\geq 1}(p_T^{\text{jet}} \geq 30 \text{ GeV}, |\eta^{\text{jet}}| \leq 3.0) = (3.32 \text{ pb}) [4.7 \alpha_s + 26 \alpha_s^2 + \mathcal{O}(\alpha_s^3)] .$$

- Accidental cancellation between large corrections to total cross section and logarithms, leading to reduced scale error. No reason to persist at higher orders

Explicit demonstration

- Further evidence: three ways of extending the calculation of the 0-jet event fraction that differ by $O(\alpha_s^3)$ w.r.t. leading order



Banfi, Salam, Zanderighi 2012

$$f_0^{(a)}(p_T^{\text{cut}}) \equiv \frac{\Sigma^{(0)}(p_T^{\text{cut}}) + \Sigma^{(1)}(p_T^{\text{cut}}) + \Sigma^{(2)}(p_T^{\text{cut}})}{\sigma^{(0)} + \sigma^{(1)} + \sigma^{(2)}}$$

$$f_0^{(b)}(p_T^{\text{cut}}) = 1 - \frac{\sigma_{1\text{-jet}}^{\text{NLO}}(p_T^{\text{cut}})}{\sigma^{(0)} + \sigma^{(1)}}.$$

$$f_0^{(c)}(p_T^{\text{cut}}) = 1 - \frac{\sigma_{1\text{-jet}}^{\text{NLO}}(p_T^{\text{cut}})}{\sigma^{(0)}} + \frac{\sigma^{(1)}}{(\sigma^{(0)})^2} \sigma_{1\text{-jet}}^{\text{LO}}(p_T^{\text{cut}})$$

- Gives results differing from 0.5 to 0.85 for a 30 GeV veto

Error prescription

- A solution using fixed-order results was pointed out (Stewart, Tackmann 2011)

First consider *inclusive* jet cross sections

$$\sigma_{\text{total}}, \sigma_{\geq 1}, \sigma_{\geq 2} \Rightarrow C = \begin{pmatrix} \Delta_{\text{total}}^2 & 0 & 0 \\ 0 & \Delta_{\geq 1}^2 & 0 \\ 0 & 0 & \Delta_{\geq 2}^2 \end{pmatrix}$$

- In the limit of $\ln(m_H/p_{T,\text{cut}})$ large, σ_{tot} and $\sigma_{\geq 1}$ have independent expansions

Transform to *exclusive* jet cross sections

$$\sigma_0 = \sigma_{\text{total}} - \sigma_{\geq 1}, \quad \sigma_1 = \sigma_{\geq 1} - \sigma_{\geq 2}, \quad \sigma_{\geq 2}$$

- Gives expected result, that $\Delta\sigma_{\text{veto}} > \Delta\sigma_{\text{tot}}$

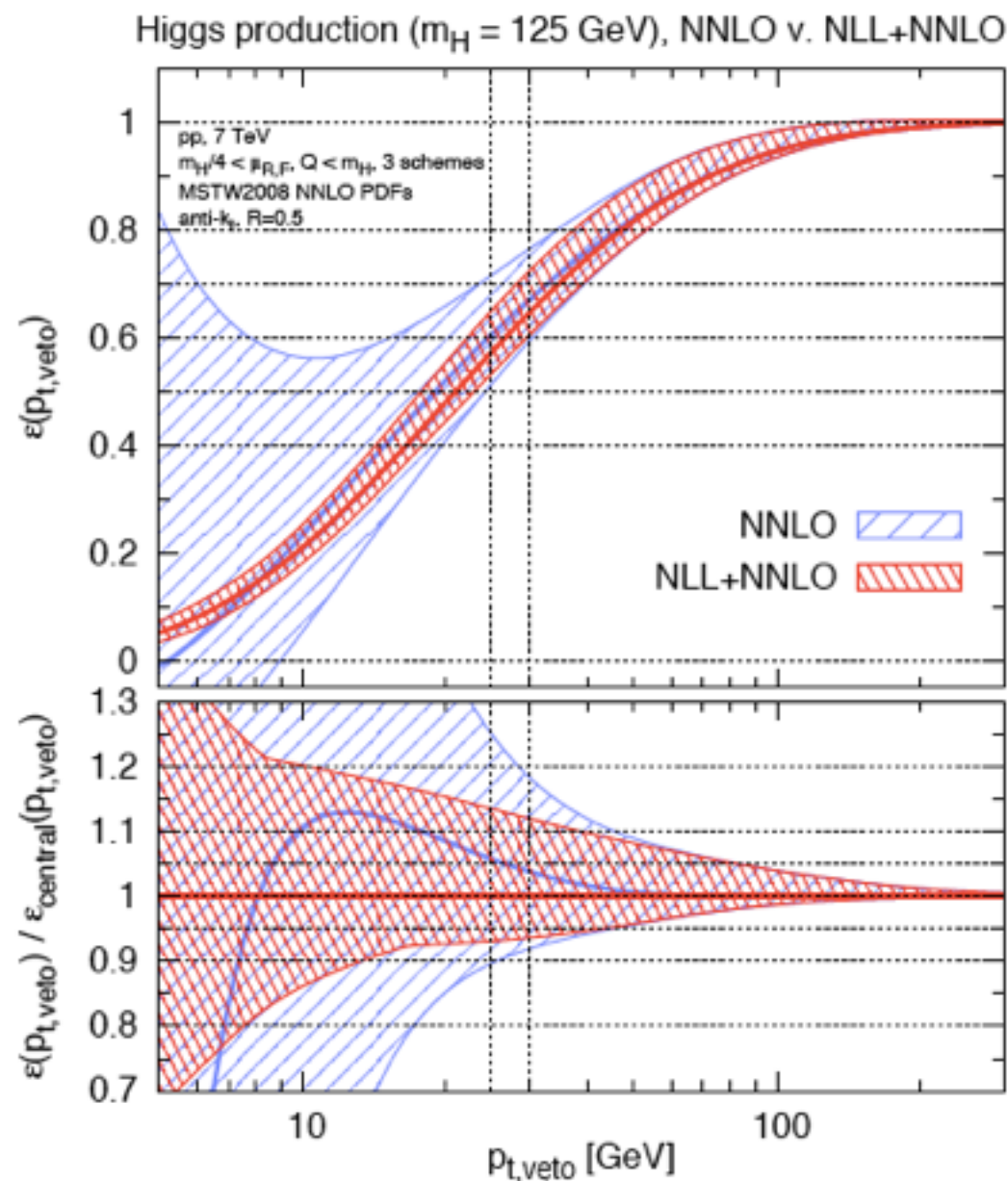
- The current prescription used in LHC analyses (phrased in terms of jet fractions)

$$\Rightarrow C = \begin{pmatrix} \Delta_{\text{total}}^2 + \Delta_{\geq 1}^2 & -\Delta_{\geq 1}^2 & 0 \\ \Delta_{\geq 1}^2 & \Delta_{\geq 1}^2 + \Delta_{\geq 2}^2 & -\Delta_{\geq 2}^2 \\ 0 & -\Delta_{\geq 1}^2 & \Delta_{\geq 2}^2 \end{pmatrix}$$

cut	$\frac{\Delta\sigma_{\text{total}}}{\sigma_{\text{total}}}$	$\frac{\Delta\sigma_{\geq 1}}{\sigma_{\geq 1}}$	$\frac{\Delta\sigma_{\geq 2}}{\sigma_{\geq 2}}$	$\frac{\Delta\sigma_0}{\sigma_0}$	$\frac{\Delta\sigma_1}{\sigma_1}$
$p_T^{\text{cut}} = 30 \text{ GeV}, \eta^{\text{cut}} = 3$	10%	21%	45%	17%	29%

Jet-veto resummed

- Recent NLL resummation of the jet-vetoed cross section
Banfi, Salam, Zanderighi 2012

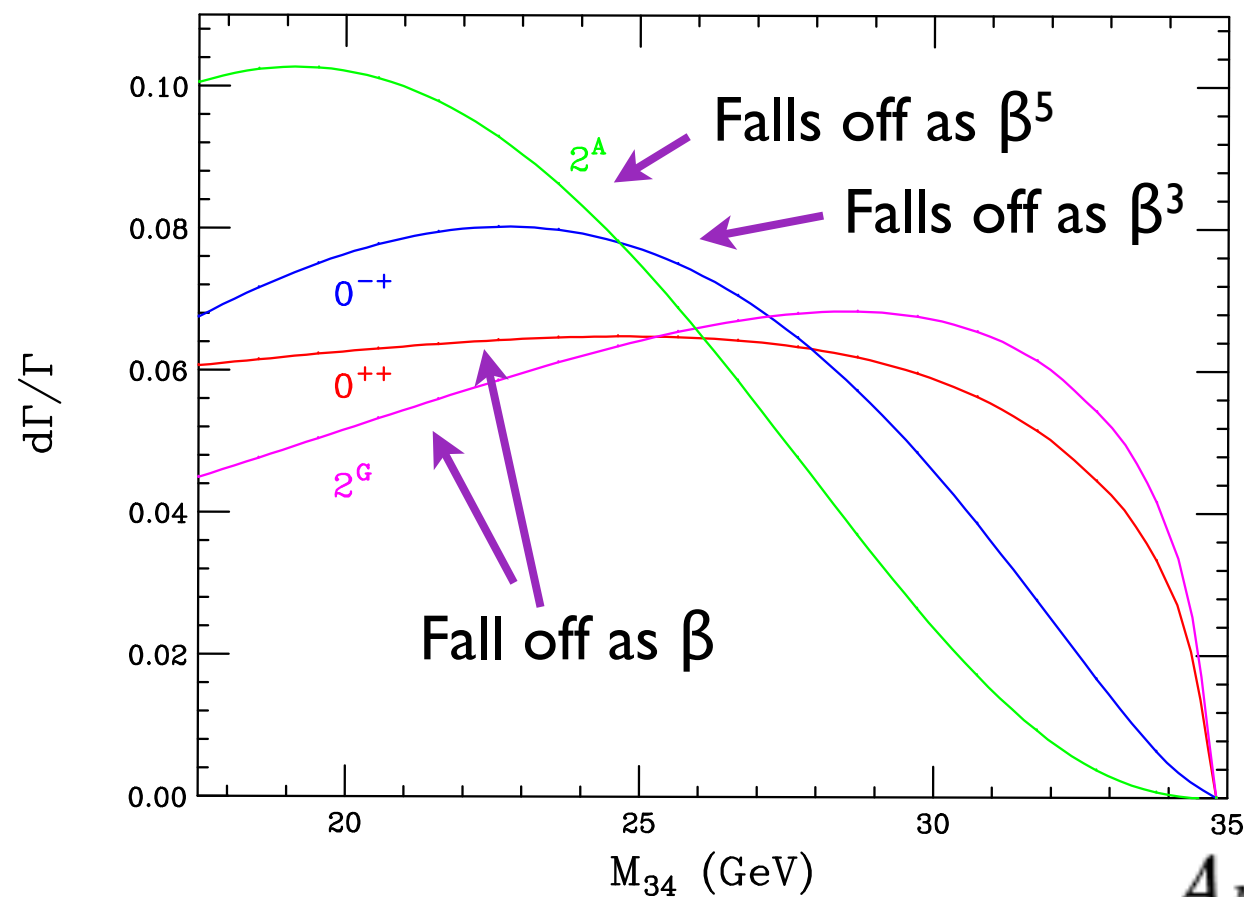


- Numbers not much reduced from those estimated using previous prescription (error defined here as envelope of methods a, b, c from before)
- Very recent attempts to extend this to NNLL by two groups: Banfi, Monni, Salam, Zanderighi; Becher, Neubert
It is an area of active debate whether this is possible: Walsh, Tackmann, Zuberi

Analyzing Higgs properties

Studying the Higgs properties using single variable asymmetries

- First establish the spin and CP properties of the new resonance; let's make sure it's the Higgs!
- In $H \rightarrow ZZ \rightarrow 4l$, with lepton-pair invariant masses M_{12} and M_{34} , the threshold behavior differs for various spin/CP combinations as M_{34} approaches its maximum $M_H - M_{12}$



R. B., LeCompte, Petriello arXiv:1208.4311

β =momentum of 34 system in Higgs rest frame

- A simple asymmetry captures this difference in shape:

$$\mathcal{A}_{M_{cut}} = \frac{N(M_{34} > M_{cut}) - N(M_{34} < M_{cut})}{N(M_{34} > M_{cut}) + N(M_{34} < M_{cut})}$$

Studying the Higgs properties using single variable asymmetries

- Results with one handful of events: [R. B., LeCompte, Petriello arXiv:1208.4311](#)

Consider an initial study of ATLAS+CMS events consistent with ZZ^* production. This is just 10 events, with half expected to be background! Note that the extension to Z^*Z^* is not difficult, not done here for simplicity of M_{cut} choice.

$$\mathcal{A}_{26}^{\text{sig}+\text{back}}(0^{++}) = -0.060, \quad \mathcal{A}_{26}^{\text{sig}+\text{back}}(2^A) = -0.31 \quad A_{26}(\text{data}) = 0 \pm 0.28$$

\Rightarrow already disfavor 2^A at the $1-\sigma$ level

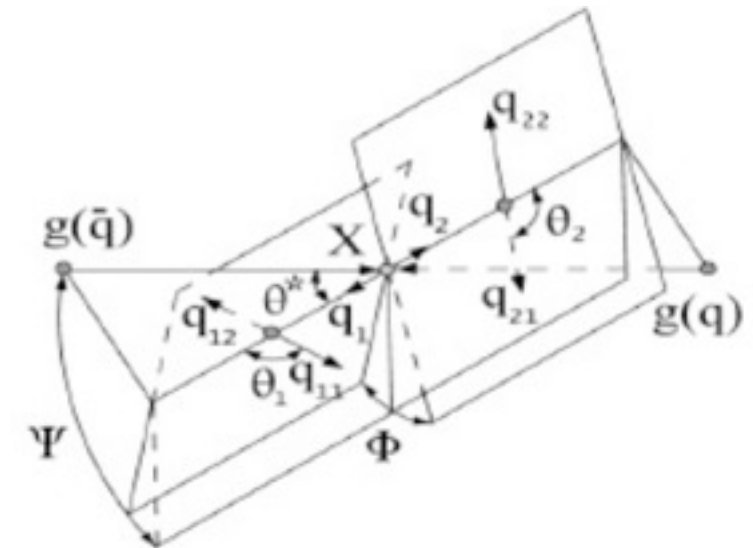
$$\mathcal{A}_{28}^{\text{sig}+\text{back}}(0^{++}) = -0.31, \quad \mathcal{A}_{28}^{\text{sig}+\text{back}}(0^{-+}) = -0.44 \quad A_{28}(\text{data}) = -0.40 \pm 0.27$$

\Rightarrow data uncertainty too large right now, need more luminosity

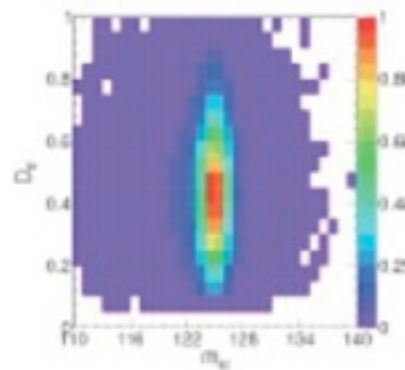
- The method has the advantage of simplicity, ease of application with the initial data, and ability to trivially combine ATLAS and CMS data

Studying the Higgs properties using MELA

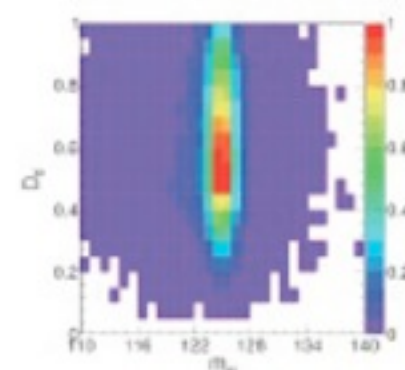
- Spin and parity are explored through angular analysis of Higgs decay products in $H \rightarrow WW, ZZ, \gamma\gamma$
- To enhance hypothesis separation, a multi-variate analysis (MELA) was developed



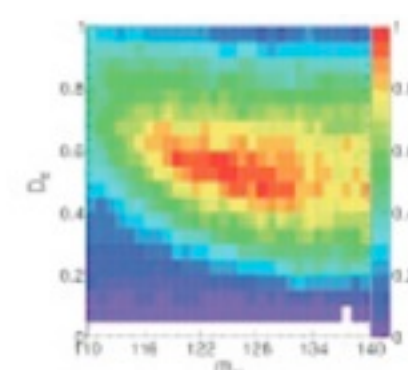
2-dim. analysis
MELA vs. m_{4l}



SM Higgs



spin-0 pseudoscalar



SM background

Expected separation significance (Gaussian σ) for 35 fb⁻¹ integrated luminosity at the 8 TeV LHC

scenario	$X \rightarrow ZZ$	$X \rightarrow WW$	$X \rightarrow \gamma\gamma$	combined
0_m^+ vs background	7.1	4.5	5.2	9.9
0_m^+ vs 0^-	4.1	1.1	0.0	4.2
0_m^+ vs 2_m^+	1.6	2.5	2.5	3.9

JHU generator
Bolognesi et al

Summary

- We have moved beyond the discovery stage of the Higgs and begun analyzing the discovered particle
- SM predictions for the Higgs are the benchmark against which all other possibilities will be compared
- After years of work by a large community, predictions under fairly good control
- The few lingering issues occur in the interplay of experimental cuts with QCD. In general, one has to be careful with jet vetoes
- Many tools exist; recent new ones for both signal and background
- We're prepared for the next stage after discovery!

Higgs excitement has just begun, sketching the Higgs's face will require a lot of theoretical and experimental hard work!

